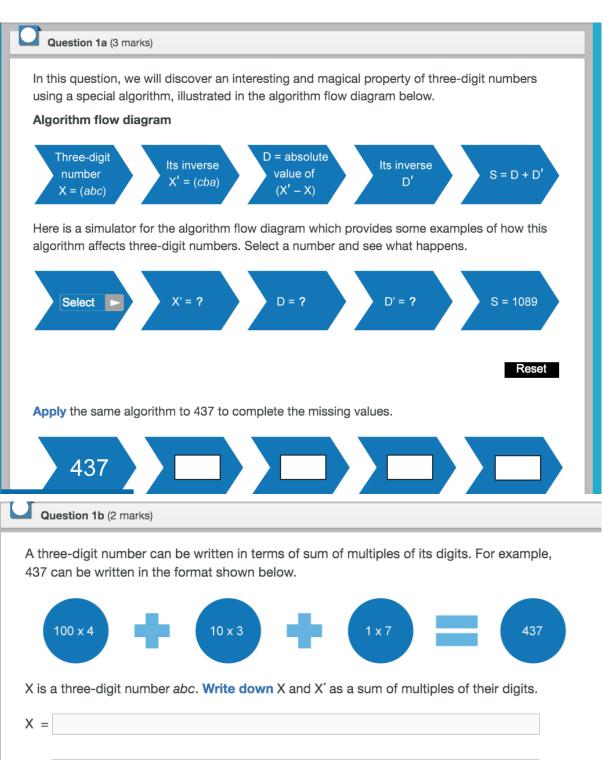
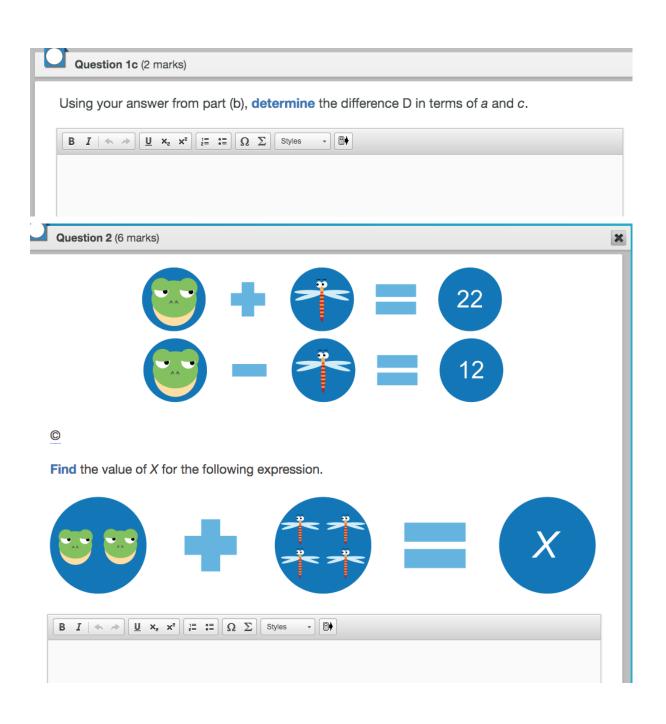
2018 May eAssessment Mathematics







To raise money for their graduation party, senior students organize a cookie and muffin sale.

x represents the number of cookies and *y* represents the number of muffins. The amount of cookies and muffins sold are represented by the shaded region in the diagram below.

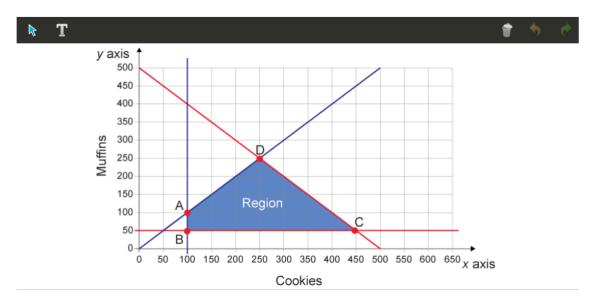
Using the information provided in the diagram below:

- Identify the shaded region by completing the inequalities below.
- The first constraint is that they cannot sell more than a total of 500 cookies and muffins. **State** the other three constraints in the spaces provided.

Draggable inequalities	Ineq	ualities	Constraints
≥	x + y	∕ ≤ 500	Total number of cookies and muffins cannot exceed 500
≤	х	100	
2	У	50	
	У	х	

Diagram

Diagram





The profit P, in Canadian dollars (CAD), for the cookies and muffins sale is calculated using the formula P = x + 1.5y.

Interpret the meaning of the coefficients of *x* and *y* in the profit formula above.



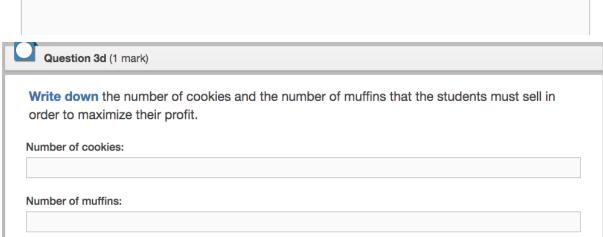


The table below shows the profit at the vertices A, B and D.

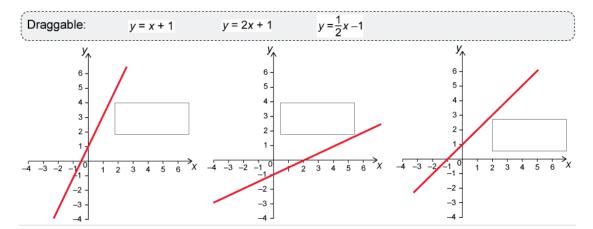
Vertices (x, y)	P = x + 1.5y (CAD)
A (100, 100)	250
B (100, 50)	175
С	
D (250, 250)	625

Determine the missing profit at vertex C.

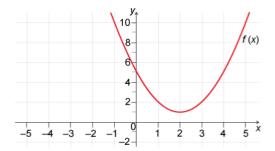




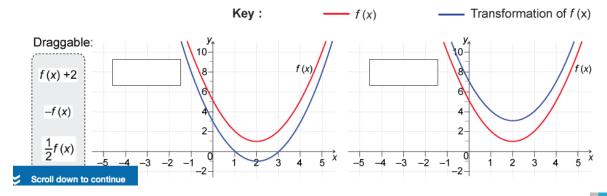
Select the line equations and place them with the corresponding graphs.



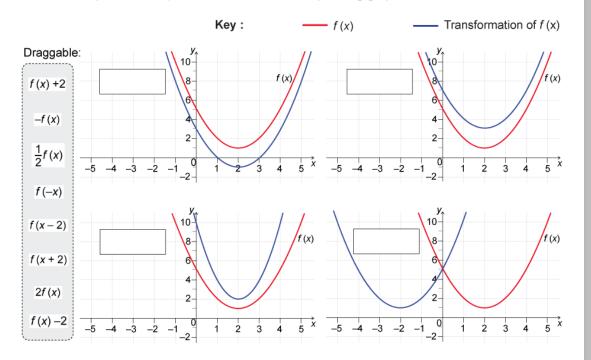
The graph below represents the function f(x). Transformations of f(x) are shown in the following graphs.

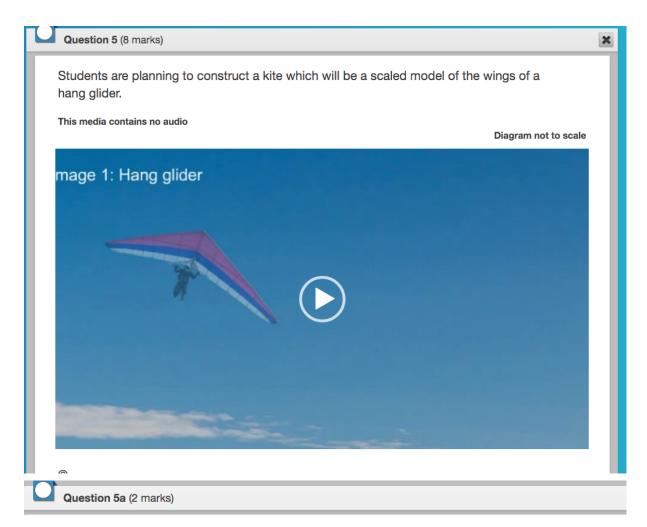


Select the equations and place them with the corresponding graphs.



Select the equations and place them with the corresponding graphs.

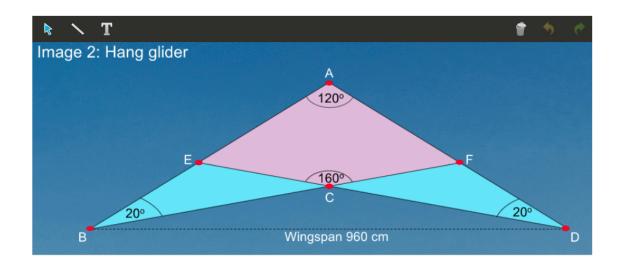


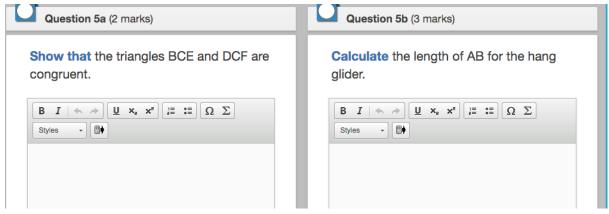


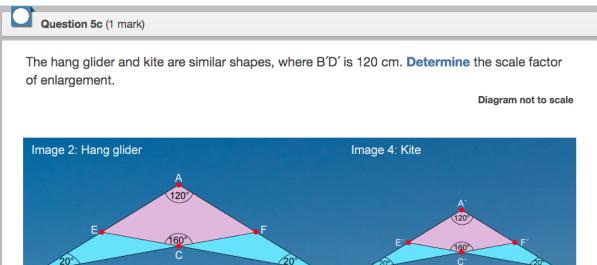
The hang glider is a quadrilateral with the following properties:

Sides	Angles	
AB = AD	ABC = ADC = 20°	
BC = DC	ECF = 160°	
BD = 960 cm	BAD = 120°	

Diagram not to scale







Question 5d (2 marks)

The area of the hang glider is 92 395 cm².

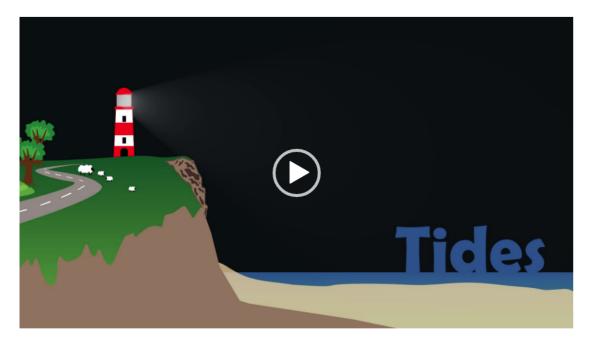
Wingspan 960 cm

Determine the area of the kite.



Wingspan 120 cm

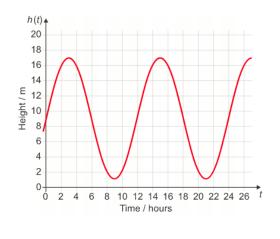
The following video illustrates how tidal range can be modelled over time by a sine function.



0

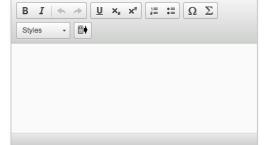
Below is the sine curve modelling the tide in Saint-Malo on a day in November 2017.

h(t) is the height in metres (m) of water in the harbour and t is the number of hours after midnight.



Question 6a (2 marks)

Determine the tidal range which is the difference between the height of the low and high tides in the harbour.

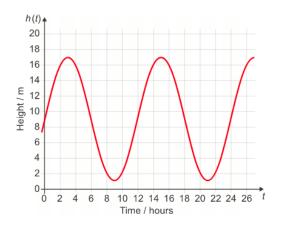


Question 6b (2 marks)

The <u>period</u> can be measured as the time difference between two consecutive high tides. **Determine** the period of this tide.

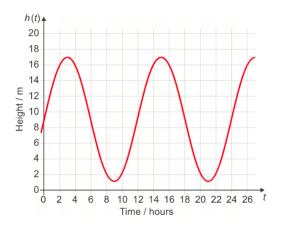
Below is the sine curve modelling the tide in Saint-Malo on a day in November 2017.

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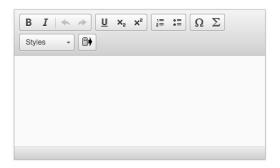
Below is the sine curve modelling the tide in Saint-Malo on a day in November 2017.

h(t) is the height in metres (m) of water in the harbour and t is the number of hours after midnight.





Using the graph, estimate at what times, during the first 12 hours after midnight, the height of the water is 2 m.





Question 6d (2 marks)

The behaviour of this tide can be modelled by the function

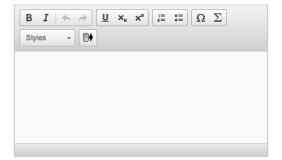
 $h(t) = a\sin(30t) + c.$

Using the graph characteristics, justify that a = 8 and c = 9.

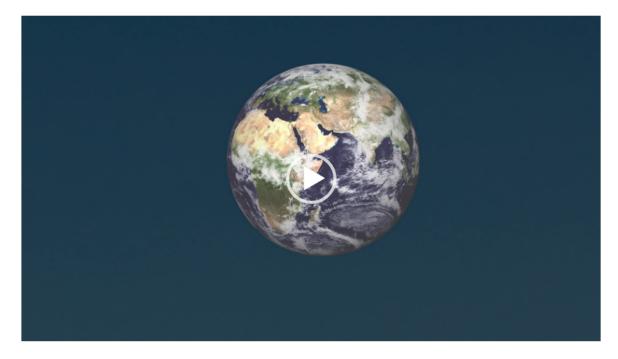


Question 6e (2 marks)

By substituting into the equation $h(t) = 8\sin(30t) + 9$, calculate the height in metres of water in the harbour at 17:00.



The following video shows how mathematics can be used to make predictions for population growth over time and space.



0

Use the table in Tab 1 below to answer questions (a), (b) and (c).

The table below shows the age distribution of the population of Australia (percentage to nearest 1 %, data correct as at 2015).

Age (A)	Percentage
0 < A ≤ 20	23
20 < A ≤ 40	32
40 < A ≤ 60	27
60 < A ≤ 80	17
80 < A ≤ 100	1

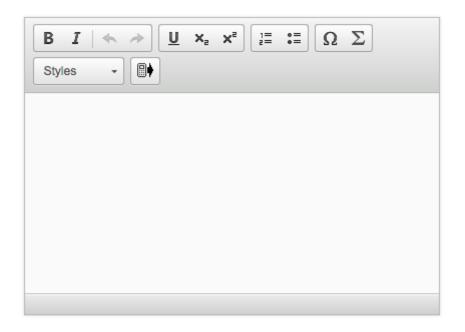
Tab 2

The table below shows the country of birth of immigrants to Australia (data correct as at 2015, top ten countries only).

Country of birth	Number of immigrants	
United Kingdom	1 207 000	
New Zealand	611 400	
China	481 800	
India	432 700	
Philippines	236 400	
Vietnam	230 200	
Italy	198 200	
South Africa	178 700	
Malaysia	156 500	
Germany	125 900	



Write down the modal class for the age distribution in Australia.

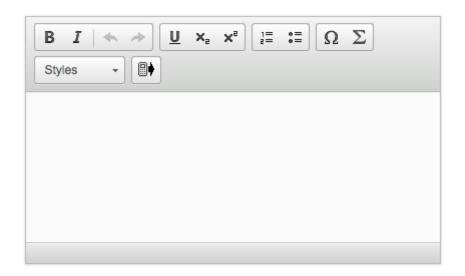




Show that the estimated mean age is 38.2



A person was selected at random from the population of Australia in 2015. **Determine** the probability that this person was over 60 years old.





The total population of Australia in 2015 was estimated to be 23 858 000 to the nearest 1000. Using the data in Tab 2, show that 5 % of the Australian population were immigrants from the United Kingdom (UK), to the nearest percent.



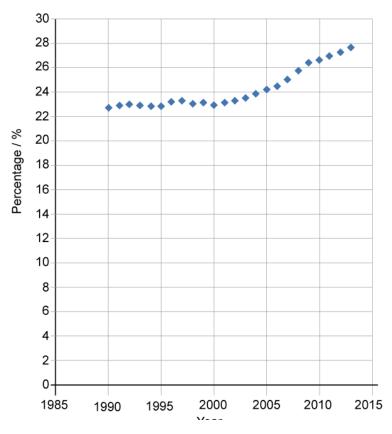
A person was selected at random from the population of Australia in 2015. **Determine** the probability that this person was an immigrant from the UK over 60 years old.

The graph below shows immigrants as a percentage of the population of Australia from 1990 to 2013.

Draw a line of best fit on the graph.



Immigrants as a percentage of the population



Scroll down to continue

AUSTRALIAN NEWS

IMMIGRANTS IN AUSTRALIA

WILL EXCEED THE NATIVE

POPULATION BY 2050





Analyse the information provided to comment on this news headline.

In your answer, you should:

- identify the factors to be considered when making your prediction
- estimate in what year the percentage of immigrant population in Australia will exceed 50 %
- · use a suitable degree of accuracy for your results
- justify whether the year you estimated makes sense in the context of the problem
- · comment on the news headline.

Tab 2

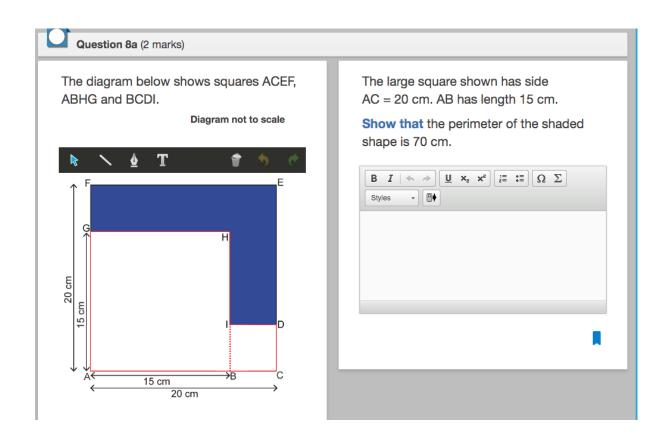
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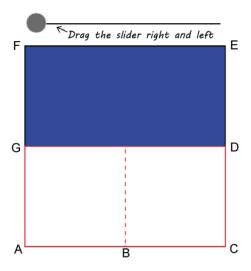


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Malaysia	156 500	
Germany	125 900	



On the simulator below, use the slider to change the length of AB and see the corresponding length of the perimeter of the shaded shape when AC is 20 cm.



Length of AB	Perimeter of shaded shape / cm	
10	60	

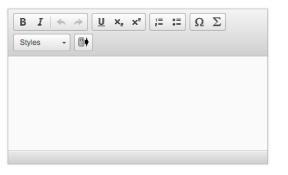
Question 8c (1 mark)

Question 8b (1 mark)

Write down the missing values in the table when the length of AB is L = 14 cm.

Length of AC, in cm	Length of AB (L) in cm	Length of BC in cm	Perimeter of shaded shape (P) in cm
20	10	10	60
20	11	9	62
20	12	8	64
20	13	7	66
20	14		
20	15	5	70
20			

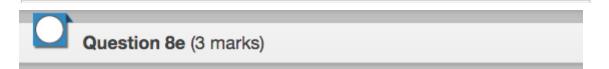
Write down, in words, a pattern from the table for the perimeter (P).



Reset

Question 8d (2 marks)

Determine a general rule for (P), the perimeter of the shaded shape, in terms of (L), the length of AB.



Verify your general rule.



Traditional shoemakers used a tool as shown below.

Click on "Start" to illustrate the shapes studied by ancient Greeks based on the shoemaker tool.

Start



Traditional shoemakers tool

Diagram not to scale

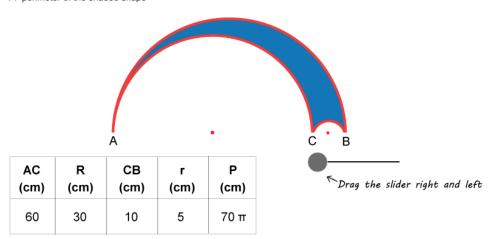
The diameter AB is 100 cm. The radius of semi-circle AC is 30 cm and radius of semi-circle CB is 20 cm.

Show that the perimeter of the shaded shape is 100π .

On the simulator below, use the slider to change the diameter CB and see the corresponding length of the perimeter of the shaded shape.

Key:

- D: diameter of the semi-circle AB
- R: radius of the semi-circle AC, which is 30 cm
- r: radius of the semi-circle CB
- P: perimeter of the shaded shape



Investigate the relationship between the radius (r) of semi-circle CB and the perimeter (P) of the shaded shape when radius of semi-circle AC is 30 cm. You may use the simulator above. In your answer, you should:

- · predict more values for P
- · write down, in words, any patterns you see for P
- find a general rule for the perimeter of the shaded shape (P) in terms of (r)
- · test your general rule
- · prove or verify and justify your general rule
- ensure that you communicate the above appropriately.

To support your investigation, you may record data in the table below.

	_	
R	r	Р
30	5	70 π
30	10	80 π
30	15	90 π
30	20	100 π
30	25	π
30	30	π
30		π
30		π
		π
		π

